Math 231 **Quiz #4** **Fall 2023** **Name:**

1. Find the general solution to $y'' - 3y' + 2y = 0$.

Solution. Solve $r^2 - 3r + 2 = 0$ get $r_1 = 1$ and $r_2 = 2$.

$$y = C_1 e^t + C_2 e^{2t}$$

2. Find the general solution to $y'' - 3y' + 2y = e^t$

Solution. Since e^t is a solution to the homogeneous equation. So we set up $y_p = Ate^t$. Then $y_p' = Ae^t(1 + t)$ and $y_p" = Ae^t(t + 2)$.

$$y_p'' - 3y_p' + 2y_p = Ae^t\Big((t + 2) - 3(t + 1) + 2t\Big) = -Ae^t$$

Solve $-Ae^t = e^2$ we have $A = -1$. Hence, $y_p = -te^t$. The general solution is

$$y = C_1 e^t + C_2 e^{2t} - te^t$$