

$$5. \quad R = (\cos t + \sin t) \hat{i} + (\sin t - \cos t) \hat{j} + \frac{1}{2}t \hat{k}$$

$$(a) \quad V = \frac{dR}{dt} = (-\sin t + \cos t) \hat{i} + (\cos t + \sin t) \hat{j} + \frac{1}{2} \hat{k}$$

$$|V| = \sqrt{1+1+\frac{1}{4}} = \frac{3}{2}$$

$$(b) \quad \vec{a} = \frac{d^2 R}{dt^2} = (-\cos t + (-\sin t)) \hat{i} + (-\sin t + \cos t) \hat{j} + 0 \cdot \hat{k}$$

$$\vec{a} = -\cos t (\hat{i} - \hat{j}) - \sin t (\hat{i} + \hat{j})$$

$$(c) \quad T = \frac{V}{|V|} = \frac{2}{3} [(-\sin t + \cos t) \hat{i} + (\cos t + \sin t) \hat{j} + \frac{1}{2} \hat{k}]$$

$$(d) \quad \kappa = \frac{\left| \frac{dT}{dt} \right|}{\frac{ds}{dt}} = \frac{\frac{2}{3} \cdot \sqrt{2}}{\frac{3}{2}} = \frac{4}{9} \sqrt{2}$$

$$\text{Since } \frac{dT}{dt} = \frac{2}{3} [(-\cos t - \sin t) \hat{i} + (-\sin t + \cos t) \hat{j} + 0 \cdot \hat{k}]$$

(e) If we change the axis.

$$\text{Let } \hat{i}' = \hat{i} - \hat{j}, \quad \hat{j}' = \hat{i} + \hat{j}$$

$$\text{then } R = \cos t \hat{i}' + \sin t \hat{j}' + \frac{1}{2}t \hat{k}$$

$\therefore$ the curve is a helix.