

1. Let $f(x, y) = -x^5 + y^5 + 5x^2y$

- (a) [8 points] What is the slope of the tangent line in the x -direction at $(1, 1)$? In the y -direction?

slope of tan. line in x -direction = $f_x(1, 1)$
@ $(1, 1)$

$$f_x(x, y) = -5x^4 + 10xy$$

$$f_x(1, 1) = -5 + 10 = 5$$

slope of tan. line in y -direction = $f_y(1, 1)$

$$f_y(x, y) = 5y^4 + 5x^2 \Rightarrow f_y(1, 1) = 5 + 5 = 10 = m_y$$

- (b) [10 points] Give the equation of the tangent plane to $f(x, y)$ at $(1, 1)$.

tan. plane at (a, b) :

$$z = f(a, b) + f_x(a, b)(x - a) + f_y(a, b)(y - b)$$

if $(a, b) = (1, 1) \Rightarrow z = 5 + 5(x - 1) + 10(y - 1)$

- (c) [6 points] Use the tangent plane equation to estimate $f(1.1, 0.9)$.

$$\begin{aligned} f(1.1, 0.9) &\approx \text{tan plane height @ } (1.1, 0.9) \\ &= 5 + 5(1.1 - 1) + 10(0.9 - 1) \\ &= 5 + 0.5 + (-1) \\ &= 4.5 \end{aligned}$$