

1. Evaluate the following indefinite integrals:

- $\int \sqrt{e^x} dx$
- $\int \frac{\sqrt{q^3}}{\sqrt[3]{q^2}} dq$
- $\int 0 dx$
- $\int (2x + 1)^2 dx$
- $\int e^{x^2} dx$

2. Suppose the growth rate of Liz's army  $t$  turns after starting a new game of Civ is given by  $A(t) = 2 \ln(t + 4)$ , and she starts the game with 3 units in her military. Use a Riemann sum with  $n$  subintervals to approximate the size of her army after 200 turns, for  $n = 5$ ,  $n = 10$ ,  $n = 100$ , and  $n = 999$ . Write out the complete sum for the first approximation, and identify  $a$ ,  $b$ ,  $\Delta x$ , and  $x_0, \dots, x_{n-1}$  in all four cases.
3. Suppose the depth of the water table  $t$  days after the start of a drought is increasing at a rate given (in ft/day) by  $r(t) = \frac{3}{\sqrt{t}}$ . Determine how deep the water table was at the start of the drought if it was 20 feet deep after 3 weeks, and determine when the water table will reach a depth of 25 feet.
4. Find the exact value of the area enclosed by the graphs of  $f(x) = x^4$  and  $g(x) = x^5$ .
5. Suppose a cook kneads a wad of pasta dough from 7:01-7:11 P.M., and the growth rate of Gluten in the dough  $t$  minutes after 7:00 P.M. is given (in grams/minute) by  $G(t) = \frac{35}{t}$ . Find  $\int_1^{11} G(t) dt$  using FTC. Give units and interpret your answer.
6. Find the producer and consumer surplus for a product with supply and demand curves given by  $s(x) = 10\sqrt{x}$  and  $d(x) = 110 - \sqrt{x}$ .
7. Find the average value of  $f(x) = \sqrt{x}$  on the interval  $[4, 16]$ .
8. Find

$$\int \frac{e^{\sqrt[3]{x}}}{\sqrt[3]{x^2}} dx$$