

## section 6:

- finding limits
- algebraic method
- limits as  $x \rightarrow \pm\infty$

## section 7:

- continuity: definition:  $\lim_{x \rightarrow a} f(x) = f(a)$
- types of discontinuities: removable, jump, vertical asymptote
- Sign Chart Method

## section 8:

- derivatives: both definitions:  

$$f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a} \quad \text{and} \quad f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$
- power rule:  $D_x x^k = kx^{k-1}$ ,  $D_x (f(x))^k = k(f(x))^{k-1}$

## section 9:

- derivative formulas
- sum rule:  $D_x (a \cdot f(x) + b \cdot g(x)) = a \cdot f'(x) + b \cdot g'(x)$
- product rule:  $D_x (f(x)g(x)) = f'(x)g(x) + f(x)g'(x)$
- quotient rule:  $D_x \frac{f(x)}{g(x)} = \frac{g(x)f'(x) - f(x)g'(x)}{(g(x))^2}$
- reciprocal rule:  $D_x \frac{1}{g(x)} = -\frac{g'(x)}{(g(x))^2}$

## section 10:

- chain rule:  $D_x g(f(x)) = g'(f(x))f'(x)$

## section 11:

- time derivatives
- velocity:  $v(t) = y'(t)$  and acceleration:  $a(t) = v'(t) = y''(t)$
- growth rates

## section 12:

- graphing
- critical points:  $y' = 0$
- relative maxima and minima
- First Derivative Test
- asymptotes

## section 13:

- second derivative
- concavity
- inflection points:  $y'' = 0$
- Second Derivative Test

## section 14:

- finding the absolute maximum and minimum over an interval
- Sole Critical Point Test
- optimal design: objective functions and constraints

## section 16:

- derivatives of exponential functions:  $D_t e^t = e^t, D_t e^{f(t)} = f'(t)e^{f(t)}$
- derivatives of logarithmic functions:  $D_x \ln x = \frac{1}{x}, D_x \ln f(x) = \frac{f'(x)}{f(x)}$

## section 17:

- exponential growth/decay:
  - $N' = rN, N(0) = N_0 \Rightarrow N(t) = N_0 e^{rt}$
  - $N' = -rN, N(0) = N_0 \Rightarrow N(t) = N_0 e^{-rt}$
  - $y' = ky, y(0) = y_0 \Rightarrow y(t) = y_0 e^{kt}$
- doubling-time:  $t_d = \frac{\ln 2}{r}$  / half-life:  $t_h = \frac{\ln 2}{r}$
- per capita growth rate:  $PCGR = \frac{1}{N} \frac{dN}{dt}$
- Newton's Law of Cooling:  
 $T'(t) = -k(T - T_{room}), T(0) = T_{init} \Rightarrow T(t) = T_{room} + (T_{init} - T_{room})e^{-kt}$

## section 18:

- antiderivatives: formulas
- solving differential equations (DEs) with and without boundary conditions (BCs)

## section 19:

- finding area by summation:  $A = \lim_{\Delta x \rightarrow 0} \sum f(x)\Delta x$

## section 20:

- the Fundamental Theorem of Calculus:  $\int_a^b f(x)dx = F(x)\Big|_a^b = F(b) - F(a)$
- finding the area under a curve using integrals
- converting a rate of change (ex. velocity) into an amount of change (ex. distance traveled)

## section 21:

- average value of a function:  $\bar{f} = \frac{1}{b-a} \int_a^b f(x) dx$
- area between two curves:  $A = \int_a^b (f(x) - g(x)) dx$
- volume of a solid of revolution:  $V = \pi \int_a^b (f(x))^2 dx$

## section 22:

- u-substitution
- method of partial fractions

## section 24:

- integration by parts:  $\int wv' dx = wv - \int w'v dx$

## section 29:

- trigonometric functions
- fitting data to the generalized sine function:  $y = B + A \sin(\omega(t - t_0))$
- solving  $\sin \theta = k$  and  $\cos \theta = k$

## section 30:

- derivative and integrals of the trigonometric and inverse trigonometric functions
- finding minima and maxima:  $N' = 0$
- finding maximum and minimum growth rates:  $N'' = 0$

## section 31:

- triangle trigonometry
- optimization problems

## section 32:

- implicit differentiation
- related rates
- allometric relationships:

$$\frac{1}{y} \frac{dy}{dt} = k \frac{1}{x} \frac{dx}{dt}, y(0) = y_0, x(0) = x_0 \Rightarrow y = \frac{y_0}{(x_0)^k} x^k = y_0 \left( \frac{x}{x_0} \right)^k$$

## section 33:

- separation of variables:  $\frac{dy}{dt} = f(y)g(t) \Rightarrow \int \frac{1}{f(y)} dy = \int g(t) dt$
- finding minima and maxima:  $N' = 0$
- finding maximum and minimum growth rates:  $N'' = 0$