

3.3 pg 107

#4  $T_0 = 10^\circ\text{C}$ ,  $M = 23^\circ\text{C}$

Given  $T(10) = 15^\circ\text{C}$ ,  $t = ?$  for  $T = 18^\circ\text{C}$

NLC  $T = T(t) = M + (T_0 - M)e^{kt}$

The given info is needed to determine  $k$ ,  
the heat transfer coefficient.

$$15 = 23 + (10 - 23)e^{10k}$$

$$\frac{-8}{-13} = e^{10k} \Rightarrow k = \frac{\ln\left(\frac{8}{13}\right)}{10}$$

$$k \approx -0.0485507816 \text{ s}^{-1}$$

How long then till the wine warms to  $18^\circ\text{C}$

$$18 = 23 + (10 - 23)e^{kt}$$

$$-5 = -13e^{kt}$$

$$\frac{5}{13} = e^{kt} \Rightarrow t = \frac{\ln\left(\frac{5}{13}\right)}{k}$$

$$t \approx 19.68066041 \text{ min.}$$