Homework Set \# 4 - Math 371 - Fall 2009
No Quiz! Will be included in exam on $9 / 22$

1. Suppose you have the data set $\{(1,10),(2,15),(4,8),(5,2),(7,12)\}$. Use this data for the following parts:
(a) Find the full interpolation polynomial of degree 4 determined by these five points.
(b) Find the piecewise linear interpolation polynomial for these five points.
(c) Find the shape-preserving piecewise cubic polynomial that fits these five points, with $d_{1}=d_{5}=0$ end conditions.
(d) Find the cubic spline piecewise polynomial, with "not a knot" spline end conditions for these five points.
2. Now consider a set of 5 generic coordinates $\left\{\left(x_{i}, y_{i}\right) \mid i=1, \ldots, 5\right\}$, with $h_{k}=x_{k+1}-x_{k}=h$ where $h$ is a positive constant. Set up the system of 5 equations for the 5 unknown slopes $d_{1}, \ldots, d_{5}$ as a matrix problem $A \vec{d}=\vec{y}$ for
(a) the "Natural Cubic Spline" - i.e. where $P_{1}^{\prime \prime}\left(x_{1}\right)=P_{n-1}^{\prime \prime}\left(x_{n}\right)=0$
(b) the "Clamped Cubic Spline" with $d_{0}=d_{5}=0$.
(Note: you just need to find $A$ and $\vec{y}$, but do not need to solve the system)
