

$$\underline{\underline{37.}} \quad ty'' - (t+1)y' + y = t^2$$

$$\underline{\underline{\text{Try:}}} \quad y_p = v_1 e^t + v_2(t+1)$$

$$\text{where } v_1' e^t + v_2'(t+1) = 0$$

$$\text{and we get } v_1' e^t + v_2' = \frac{t^2}{t} = t$$

$$\text{subtracting these eqns} \Rightarrow v_2' t = -t \quad \text{or } v_2' = -1$$

$$\Rightarrow \boxed{v_2 = -t}$$

$$\text{Then } v_1' = +(t+1)e^{-t}$$

$$v_1 = \int (t+1)e^{-t} dt$$

$$u = t+1 \quad du = dt$$

$$dv = e^{-t} \Rightarrow v = -e^{-t}$$

$$= -(t+1)e^{-t} + \int e^{-t} dt = -(t+1)e^{-t} - e^{-t}$$

$$\text{or } \boxed{v_1 = -te^{-t} - 2e^{-t}}$$

$$\text{so } y_p = (-t-2) + (-t^2-t) = -t^2 - 2t - 2$$

and the gen. sol'n is

$$\boxed{y = c_1 e^t + c_2(t+1) - t^2 - 2t - 2}$$